# PLTW Engineering Formula Sheet 2015 (v15.0)

#### 1.0 Statistics

#### Mean

$$\mu = \frac{\sum x_i}{N}$$

(1.1a)

$$\overline{\mathbf{x}} = \frac{\sum x_i}{n} (1.1b)$$

 $\mu$  = population mean

 $\bar{x}$  = sample mean

 $\sum x_i$  = sum of all data values (x<sub>1</sub>, x<sub>2</sub>, x<sub>3</sub>, ...)

N = size of population

n = size of sample

#### Median

Place data in ascending order.

If N is odd, median = central value

(1.2)

If N is even, median = mean of two central values

N = size of population

#### **Range** (1.5)

Range =  $x_{max} - x_{min}$  (1.3)

 $x_{max} = maximum data value$ 

 $x_{min}$  = minimum data value

#### Mode

Place data in ascending order.

Mode = most frequently occurring value

(1.4)

If two values occur with maximum frequency the data set is *bimodal*.

If three or more values occur with maximum frequency the data set is *multi-modal*.

#### Standard Deviation

$$\sigma = \sqrt{\frac{\Sigma(x_i - \mu)^2}{N}}$$

(Population)

(1.5a)

$$s = \sqrt{\frac{\sum (x_i - \overline{x})^2}{n-1}}$$

(Sample)

(1.5b)

 $\sigma$  = population standard deviation

s = sample standard deviation

 $x_i$  = individual data value ( $x_1, x_2, x_3, ...$ )

 $\mu$  = population mean

 $\bar{x}$  = sample mean

N = size of population

Independent Events

n = size of sample

## 2.0 Probability

#### Frequency

$$f_x = \frac{n_x}{n_x}$$

(2.1)

#### $f_x$ = relative frequency of outcome x

 $n_x$  = number of events with outcome x

n = total number of events

## Mutually Exclusive Events

P<sub>A</sub> = probability of event A

 $P (A \text{ and } B \text{ and } C) = P_A P_B P_C$ 

$$P (A \text{ or } B) = P_A + P_B$$

(2.4)

(2.3)

P (A or B) = probability of either mutually exclusive event A or B occurring in a trial

P (A and B and C) = probability of independent

events A and B and C occurring in sequence

P<sub>A</sub> = probability of event A

# Binomial Probability (order doesn't matter)

$$P_k = \frac{n!(p^k)(q^{n-k})}{k!(n-k)!}$$

(2.2)

P<sub>k</sub> = binomial probability of k successes in n trials

p = probability of a success

q = 1 - p = probability of failure

k = number of successes

n = number of trials

#### Conditional Probability

$$P(A|D) = \frac{P(A) \cdot P(D|A)}{P(A) \cdot P(D|A) + P(\sim A) \cdot P(D|\sim A)}$$
(2.5)

P(A|D) = probability of event A given event D

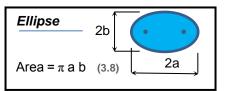
P(A) = probability of event A occurring

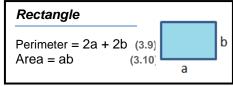
 $P(\sim A)$  = probability of event A not occurring

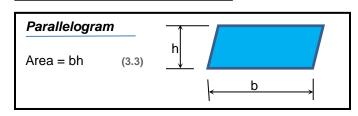
 $P(D|\sim A)$  = probability of event D given event A did not occur

## 3.0 Plane Geometry

## Circle Circumference = $2 \pi r$ (3.1) Area = $\pi$ r<sup>2</sup>

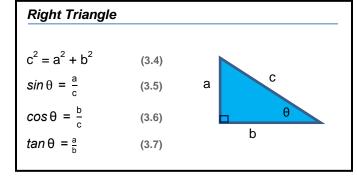


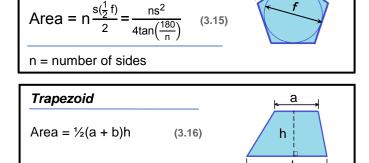




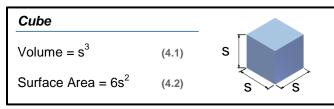
Triangle (3.6)		В
Area = ½ bh	(3.11)	a h c
$a^{2} = b^{2} + c^{2} - 2bc \cdot cos \angle A$ $b^{2} = a^{2} + c^{2} - 2ac \cdot cos \angle B$ $c^{2} = a^{2} + b^{2} - 2ab \cdot cos \angle C$	(3.13)	C b A

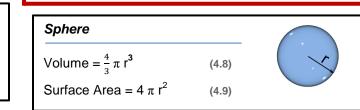
Regular Polygons

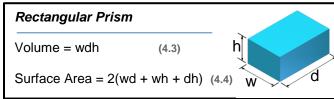


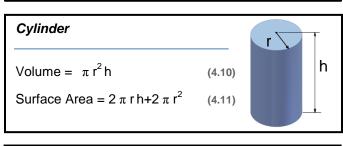


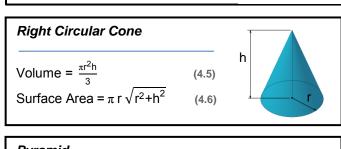
# 4.0 Solid Geometry

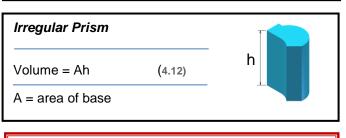












# **Pyramid** Volume = $\frac{Ah}{3}$ h (4.7)A = area of base

## 6.0 Conversions

#### Mass/Weight (6.1)

1 kg =  $2.205 \text{ lb}_{\text{m}}$ 1 slug =  $32.2 \text{ lb}_{\text{m}}$ 1 ton = 2000 lb1 lb = 16 oz

#### Length (6.2)

1 m = 3.28 ft 1 km = 0.621 mi 1 in. = 2.54 cm 1 mi = 5280 ft 1 yd = 3 ft

## Time (6.3)

1 d = 24 h 1 h = 60 min 1 min = 60 s 1 yr = 365 d

#### Area (6.4)

1 acre =  $4047 \text{ m}^2$ =  $43,560 \text{ ft}^2$ =  $0.00156 \text{ mi}^2$ 

#### Volume (6.5)

1L = 0.264 gal = 0.0353 ft<sup>3</sup> = 33.8 fl oz 1mL = 1 cm<sup>3</sup> = 1 cc

#### Temperature <u>Unit</u> Equivalents (6.6)

1 K = 1 °C = 1.8 °F = 1.8 °R

#### Force (6.7)

1 N = 0.225 lb1 kip = 1,000 lb

#### Pressure (6.8)

1 atm = 1.01325 bar = 33.9 ft  $H_2O$ = 29.92 in.  $H_3$ = 760 mm  $H_3$ = 101,325 Pa = 14.7 psi 1psi = 2.31 ft of  $H_2O$ 

#### Power (6.9)

1 W = 3.412 Btu/h = 0.00134 hp = 14.34 cal/min = 0.7376 ft·lb<sub>i</sub>/s 1 hp = 550 ft·lb/sec

#### Energy (6.10)

1 J = 0.239 cal=  $9.48 \times 10^{-4} \text{ Btu}$ =  $0.7376 \text{ ft} \cdot \text{lb}_f$ 1kW h = 3,600,000 J

#### Rotational Speed (6.11)

1 Hz =  $2\pi$  rad/sec

=60 rpm

## 7.0 Defined Units

1 J  $= 1 \text{ N} \cdot \text{m}$ 1 N  $= 1 \text{ kg·m} / \text{s}^2$ 1 Pa  $= 1 N / m^2$ = 1 W/A1 V 1 W = 1 J/s1Ω = 1 V/A $1 \text{ Hz} = 1 \text{ s}^{-1}$ 1 F  $= 1 A \cdot s / V$ 1 H  $= 1 V \cdot s / V$ 

## 8.0 SI Prefixes

Numbers Less Than One								
Power of 10	Prefix	Abbreviation						
10 <sup>-1</sup>	deci-	d						
10 <sup>-2</sup>	centi-	С						
10 <sup>-3</sup>	milli-	m						
10 <sup>-6</sup>	micro-	μ						
10 <sup>-9</sup>	nano-	n						
10 <sup>-12</sup>	pico-	р						
10 <sup>-15</sup>	femto-	f						
10 <sup>-18</sup>	atto-	а						
10 <sup>-21</sup>	zepto-	Z						
10 <sup>-24</sup>	yocto-	У						

Nullibers Greater Than One								
Power of 10	Prefix	Abbreviation						
10 <sup>1</sup>	deca-	da						
10 <sup>2</sup>	hecto-	h						
10 <sup>3</sup>	kilo-	k						
10 <sup>6</sup>	Mega-	M						
10 <sup>9</sup>	Giga-	G						
10 <sup>12</sup>	Tera-	Т						
10 <sup>15</sup>	Peta-	Р						
10 <sup>18</sup>	Exa-	Е						
10 <sup>21</sup>	Zetta-	Z						
10 <sup>24</sup>	Yotta-	Y						

Numbers Greater Than One

## 9.0 Equations

#### Mass and Weight

 $m = VD_m$  (9.1) W = mg (9.2)  $W = VD_w$  (9.3)

V = volume

D<sub>m</sub> = mass density

m = mass

D<sub>w</sub> = weight density

W = weight

g = acceleration due to gravity

#### **Temperature**

 $T_K = T_C + 273$  (9.4)

 $T_R = T_F + 460$  (9.5)

 $T_{F} = \frac{9}{5} T_{c} + 32 \tag{9.6}$ 

 $T_K$  = temperature in Kelvin

 $T_C$  = temperature in Celsius

 $T_R$  = temperature in Rankin  $T_F$  = temperature in Fahrenheit

#### Force and Moment

F = ma (9.7a) M = Fd (9.7b)

F = force

m = mass

a = acceleration

M = moment

d<sub>1</sub>= perpendicular distance

#### **Equations of Static Equilibrium**

 $\Sigma F_x = 0$   $\Sigma F_y = 0$   $\Sigma M_P = 0$  (9.8)

 $F_x$  = force in the x-direction  $F_y$  = force in the y-direction  $M_P$  = moment about point P

## 9.0 Equations (Continued)

#### Energy: Work

 $W = F_{\parallel} \cdot d$ 

(9.9)

W = work

 $F_{\parallel}$  = force parallel to direction of displacement

**d** = displacement

#### **Power**

$$P = \frac{E}{L} = \frac{W}{L}$$

(9.10)

 $P = \tau \omega$ 

(9.11)

P = power

E = energy

W = work

t = time

 $\tau$  = torque

 $\omega$  = angular velocity

#### **Efficiency**

Efficiency (%) =  $\frac{P_{out}}{P_{in}} \cdot 100\%$  (9.12)

 $P_{out}$  = useful power output P<sub>in</sub> = total power input

#### Energy: Potential

U = mgh

(9.13)

U = potential energy

g = acceleration due to gravity

h = height

#### Energy: Kinetic

$$K = \frac{1}{2} mv^2$$

(9.14)

K = kinetic energy

m = mass

v = velocity

#### Energy: Thermal

 $\Delta Q = mc\Delta T$ 

(9.15)

 $\Delta Q$  = change in thermal energy

m = mass

c = specific heat

 $\Delta T$  = change in temperature

#### Fluid Mechanics

$$p = \frac{F}{\Delta}$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$
 (Charles' Law) (9.17)

$$\frac{p_1}{T_1} = \frac{p_2}{T_2}$$
 (Gay-Lussanc's Law) (9.18)

$$p_1V_1 = p_2V_2$$
 (Boyle's Law) (9.19)

$$Q = Av$$

(9.20)

$$A_1 V_1 = A_2 V_2$$

(9.21)

$$P = Qp$$

(9.22)

absolute pressure = gauge pressure + atmospheric pressure (9.23)

p = absolute pressure

F = force

A = area

V = volume

T = absolute temperature

Q = flow rate

v = flow velocity

P = power

#### Mechanics

(9.24)

 $\bar{\mathbf{v}} = \frac{\Delta \mathbf{d}}{\Delta t}$ 

(9.25)

 $a = \frac{v_f - v_i}{t}$ 

(9.26)

 $X = \frac{v_i^2 \sin(2\theta)}{2\pi}$ 

(9.27)

 $v = v_i + at$ 

$$v = v_i + a_i$$

(9.28)

 $d = d_i + v_i t + \frac{1}{2} a t^2$ 

(9.29)

 $v^2 = v_i^2 + 2a(d - d_i)$ 

(9.30)

 $\tau = dFsin\theta$ 

(9.31)

 $\bar{s}$  = average speed

 $\bar{\mathbf{v}}$  = average velocity

v = velocity

 $v_i$  = initial velocity (t =0)

a = acceleration

X = range

t = time

 $\Delta \mathbf{d}$  = change in displacement

d = distance

 $d_i$  = initial distance (t=0)

g = acceleration due to gravity

 $\theta$  = angle

 $\tau$  = torque

F = force

#### **Electricity**

#### Ohm's Law

$$P = IV$$

(9.33)

$$R_T$$
 (series) =  $R_1 + R_2 + \cdots + R_n$  (9.34)

$$R_T$$
 (parallel) =  $\frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \cdots + \frac{1}{R_n}}$  (9.35)

#### Kirchhoff's Current Law

$$I_T = I_1 + I_2 + \dots + I_n$$

or 
$$I_T = \sum_{k=1}^{n} I_k$$
 (9.36)

#### Kirchhoff's Voltage Law

$$V_T = V_1 + V_2 + \cdots + V_n$$

or 
$$V_T = \sum_{k=1}^{n} V_k$$
 (9.37)

V = voltage

 $V_T$  = total voltage

I = current

 $I_T$  = total current

R = resistance

 $R_T$  = total resistance

P = power

## Thermodynamics

 $P = Q' = AU\Delta T$ 

(9.38)

 $P = Q' = \frac{\Delta Q}{\Delta t}$ 

(9.39)

 $U = \frac{1}{R} = \frac{k}{l}$ 

(9.40)

 $P = \frac{kA\Delta T}{r}$  $A_1V_1 = A_2V_2$ 

 $k = \frac{PL}{\Delta \Lambda T}$ 

(9.41)(9.42)

 $P_{net} = \sigma Ae(T_2^4 - T_1^4)$ 

(9.43)

(9.44)

P = rate of heat transfer

Q = thermal energy

A = area of thermal conductivity

U = coefficient of heat conductivity (U-factor)

 $\Delta T$  = change in temperature

 $\Delta t$  = change in time

R = resistance to heat flow (R-value)

k = thermal conductivity v = velocity

 $P_{net}$  = net power radiated

 $\sigma = 5.6696 \times 10^{-8} \frac{W}{m^2 \cdot K^4}$ 

e = emissivity constant

L = thickness

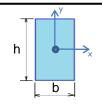
 $T_1$ ,  $T_2$  = temperature at time 1, time 2

## 10.0 Section Properties

#### Moment of Inertia

$$I_{xx} = \frac{bh^3}{12}$$

(10.1)



I<sub>xx</sub> = moment of inertia of a rectangular section about x axis

#### Complex Shapes Centroid

$$\overline{\mathbf{x}} = \frac{\sum x_i A_i}{\sum A_i}$$
 and  $\overline{\mathbf{y}} = \frac{\sum y_i A_i}{\sum A_i}$ 

(10.2)

 $\overline{x}$  = x-distance to the centroid

 $\overline{y}$  = y-distance to the centroid

 $x_i = x$  distance to centroid of shape i

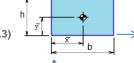
y<sub>i</sub> = y distance to centroid of shape i

 $A_i$  = Area of shape i

## Rectangle Centroid

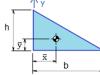
$$\bar{x} = \frac{b}{2}$$
 and  $\bar{y} = \frac{h}{2}$ 





#### Right Triangle Centroid

$$\bar{x} = \frac{b}{3}$$
 and  $\bar{y} = \frac{h}{3}$ 



#### Semi-circle Centroid

$$\bar{x} = r$$
 and  $\bar{y} = \frac{4r}{3\pi}$ 

(10.5) <u>y</u> Ţ

 $\overline{y}$ 

 $\overline{x}$  = x-distance to the centroid

 $\bar{y}$  = y-distance to the centroid

#### 11.0 Material

#### Stress (axial)

$$\sigma = \frac{F}{\Lambda}$$

(11.1)

 $\sigma$  = stress

F = axial force

A = cross-sectional area

#### Strain (axial)

$$\varepsilon = \frac{\delta}{L_0}$$

(11.2)

 $\varepsilon = strain$ 

L<sub>0</sub> = original length

 $\delta$  = change in length

## Modulus of Elasticity

$$E = \frac{\sigma}{\epsilon}$$

(11.3)

$$E = \frac{(F_2 - F_1)L_0}{(\delta_2 - \delta_1)A}$$
 (11.4)

E = modulus of elasticity

 $\sigma = stress$ 

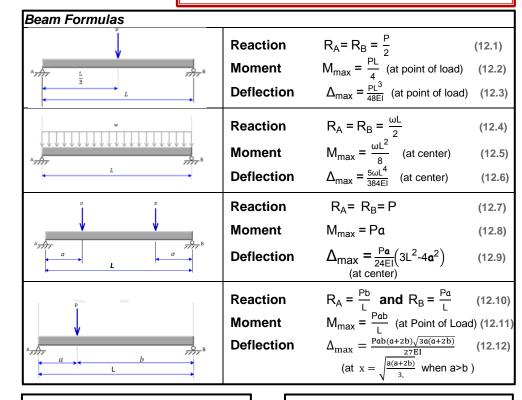
 $\varepsilon = strain$ 

A = cross-sectional area

F = axial force

 $\delta$  = deformation

## 12.0 Structural Analysis



#### Deformation: Axial

$$\delta = \frac{FL_0}{AE}$$

(12.13)

 $\delta$  = deformation

F = axial force

 $L_0$  = original length

A = cross-sectional area

E = modulus of elasticity

#### Truss Analysis

2J = M + R

(12.14)

J = number of joints

M =number of members

R = number of reaction forces

## 13.0 Simple Machines

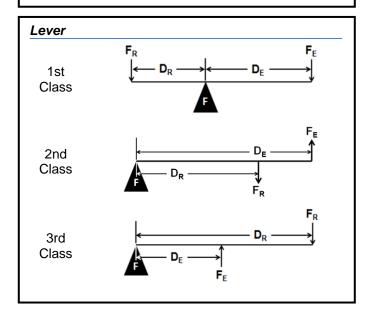
#### Mechanical Advantage (MA)

IMA= 
$$\frac{D_E}{D_R}$$
 (13.1) AMA=  $\frac{F_R}{F_E}$  (13.2)

% Efficiency= 
$$\left(\frac{AMA}{IMA}\right)$$
 100 (13.3)

IMA = ideal mechanical advantage AMA = actual mechanical advantage

 $D_E$  = effort distance  $D_R$  = resistance distance  $F_E$  = effort force  $F_R$  = resistance force



# Effort at Wheel Effort at Wheel Effort at Wheel

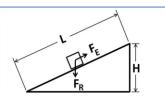
#### **Pulley Systems**

IMA = total number of strands of a single string supporting the resistance (13.4)

$$IMA = \frac{D_{E} \text{ (string pulled)}}{D_{R} \text{ (resistance lifted)}}$$
 (13.5)

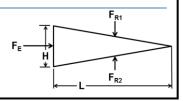
#### Inclined Plane

IMA= 
$$\frac{L}{H}$$
 (13.6)



#### Wedge

IMA= 
$$\frac{L}{H}$$
 (13.7)



#### Screw

$$IMA = \frac{C}{Pitch}$$
 (13.8)

 $Pitch = \frac{1}{TDI}$  (13.9)



C = circumference

r = radius

Pitch

Pitch = distance between

threads TPI = threads per inch

#### Compound Machines

$$MA_{TOTAL} = (MA_1) (MA_2) (MA_3) ...$$
 (13.10)

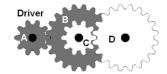
# Gears; Sprockets with Chains; and Pulleys with Belts Ratios

$$GR = \frac{N_{out}}{N_{in}} = \frac{d_{out}}{d_{in}} = \frac{\omega_{in}}{\omega_{out}} = \frac{\tau_{out}}{\tau_{in}}$$
 (13.11)

$$\frac{d_{out}}{d_{in}} = \frac{\omega_{in}}{\omega_{out}} = \frac{\tau_{out}}{\tau_{in}}$$
 (pulleys) (13.12)

## **Compound Gears**





GR = gear ratio

 $\omega_{in}$  = angular velocity - driver

 $\omega_{\text{out}}$  = angular velocity - driven

 $N_{in}$  = number of teeth - driver

N<sub>out</sub> = number of teeth - driven

d<sub>in</sub> = diameter - driver

dout = diameter - driven

 $\tau_{\text{in}}$  = torque - driver

 $\tau_{\text{out}}$  = torque - driven

## 14.0 Structural Design

#### Steel Beam Design: Shear

$$V_a \le \frac{V_n}{\Omega_v}$$

$$V_n = 0.6F_yA_w$$

V<sub>a</sub> = internal shear force

 $V_n$  = nominal shear strength

 $\Omega_{\rm v}$  = 1.5 = factor of safety for shear

 $F_v$  = yield stress

 $A_w$  = area of web

 $\frac{V_n}{V_n}$  = allowable shear strength

#### Steel Beam Design: Moment

$$M_a \le \frac{M_n}{\Omega_b}$$

$$M_n = F_v Z_x$$

M<sub>a</sub> = internal bending moment

M<sub>n</sub> = nominal moment strength

 $\Omega_b = 1.67 = factor of safety for$ bending moment

 $F_v$  = yield stress

2% to 7% slope

Light

Heavy

 $Z_x$  = plastic section modulus about neutral axis

 $\frac{M_n}{a}$  = allowable bending strength

#### Spread Footing Design

 $q_{net} = q_{allowable} - p_{footing}$ 

(14.5)

 $p_{footing} = t_{footing} \cdot 150 \frac{lb}{fr^3}$ (14.6)

(14.7)

q<sub>net</sub> = net allowable soil bearing pressure

q<sub>allowable</sub> = total allowable soil bearing pressure

p<sub>footing</sub> = soil bearing pressure due to footing weight

 $t_{footing}$  = thickness of footing

q = soil bearing pressure

P = column load applied

A = area of footing

#### 15.0 Storm Water Runoff

#### Storm Water Drainage

 $Q = C_fCiA$ 

(15.1)

$$C_{c} = \frac{C_{1}A_{1} + C_{2}A_{2} + \cdots}{A_{1} + A_{2} + \cdots}$$
(15.2)

Q = peak storm water runoff rate ( $ft^3/s$ )

C<sub>f</sub> = runoff coefficient adjustment factor

C = runoff coefficient

i = rainfall intensity (in./h)

A = drainage area (acres)

Runoff Coefficient Adjustment Factor						
Return						
Period	Period Cf					
1, 2, 5, 10	1.0					
25	25 1.1					
50	1.2					
100	1.25					

Rational Method Runoff Coefficients						
Categorized by Surface						
Forested	0.059—0.2					
Asphalt	0.7—0.95					
Brick	0.7—0.85					
Concrete	0.8—0.95					
Shingle roof	0.75—0.95					
Lawns, well draine	ed (sandy soil)					
Up to 2% slope	0.05—0.1					
2% to 7% slope	0.10—0.15					
Over 7% slope	0.15—0.2					
Lawns, poor drainage (clay soil)						
Up to 2% slope	0.13—0.17					

0.18-0.22

0.5 - 0.8

0.6 - 0.9

#### Over 7% slope 0.25 - 0.35Driveways, 0.75 - 0.85Categorized by Use Farmland 0.05 - 0.3Pasture 0.05 - 0.3Unimproved 0.1-0.3 0.1 - 0.25Parks Cemeteries 0.1 - 0.250.2 - 0.40Railroad yard Playgrounds 0.2 - 0.35**Business Districts**

Bacilloco Biotiloto						
Neighborhood	0.5—0.7					
City (downtown)	0.7—0.95					
Residential						
Single-family	0.3—0.5					
Multi-plexes,	0.4—0.6					
Multi-plexes,	0.6—0.75					
Suburban	0.25—0.4					
Apartments,	0.5—0.7					
Industrial						

## 16.0 Water Supply

#### Hazen-Williams Formula

$$h_{f} = \frac{10.44LQ^{1.85}}{C^{1.85}q^{4.8655}}$$
 (16.1)

h<sub>f</sub> = head loss due to friction (ft of  $H_2O$ )

L = length of pipe (ft)

Q = water flow rate (gpm)

C = Hazen-Williams constant

d = diameter of pipe (in.)

#### Dynamic Head

dynamic head = static head - head loss (16.2)static head = change in elevation between source and discharge

## 17.0 Heat Loss/Gain

#### Heat Loss/Gain

 $Q' = AU\Delta T$ (17.1)

 $U = \frac{1}{R}$ (17.2)

Q = thermal energy

A = area of thermal conductivity

U = coefficient of heat

conductivity (U-factor)

 $\Delta T$  = change in temperature

R = resistance to heat flow (Rvalue)

# 18.0 Hazen-Williams Constants

Pipe Material	Typical Range	Clean, New Pipe	Typical Design Value
Cast Iron and Wrought Iron	80 - 150	130	100
Copper, Glass or Brass	120 - 150	140	130
Cement lined Steel or Iron		150	140
Plastic PVC or ABS	120 - 150	140	130
Steel, welded and seamless or interior riveted	80-150	140	100

# 19.0 Equivalent Length of (Generic) Fittings

Consumal Fittings			Pipe Size										
Screwed Fitti	ngs	1/4	3/8	1/2	3/4	1	1 1/4	1 ½	2	2 ½	3	4	
	Regular 90 degree	2.3	3.1	3.6	4.4	5.2	6.6	7.4	8.5	9.3	11.0	13.0	
Elbows	Long radius 90 degree	1.5 0.3	2.0 0.5	2.2 0.7	2.3 0.9	2.7 1.3	3.2 1.7	3.4 2.1	3.6 2.7	3.6	4.0	4.6 5.5	
	Regular 45 degree						-	F	-				
Tees	Line Flow Branch Flow	0.8 2.4	1.2 3.5	1.7 4.2	2.4 5.3	3.2 6.6	4.6 8.7	5.6 9.9	7.7 12.0	9.3 13.0	12.0 17.0	17.0 21.0	
Return Bends	Regular 180 degree	2.3	3.1	3.6	4.4	5.2	6.6	7.4	8.5	9.3	11.0	13.0	
	Globe	21.0	22.0	22.0	24.0	29.0	37.0	42.0	54.0	62.0	79.0	110.0	
Mahasa	Gate	0.3	0.5	0.6	0.7	0.8	1.1	1.2	1.5	1.7	1.9	2.5	
Valves	Angle	12.8	15.0	15.0	15.0	17.0	18.0	18.0	18.0	18.0	18.0	18.0	
	Swing Check	7.2	7.3	8.0	8.8	11.0	13.0	15.0	19.0	22.0	27.0	38.0	
Strainer			4.6	5.0	6.6	7.7	18.0	20.0	27.0	29.0	34.0	42.0	

Flores d Fi	44:									Pipe	Size							
Flanged Fi	ttings	1/2	3/4	1	1 1/4	1 ½	2	2 ½	3	4	5	6	8	10	12	14	16	18
	Regular 90 degree	0.9	1.2	1.6	2.1	2.4	3.1	3.6	4.4	5.9	7.3	8.9	12.0	14.0	17.0	18.0	21.0	23.0
Elbows	Long radius 90 degree	1.1	1.3	1.6	2.0	2.3	2.7	2.7	3.4	4.2	5.0	5.7	7.0	8.0	9.0	9.4	10.0	11.0
	Regular 45 degree	0.5	0.6	0.8	1.1	1.3	1.7	2.0	2.5	3.5	4.5	5.6	7.7	9.0	11.0	13.0	15.0	16.0
Tees	Line Flow	0.7	0.8	1.0	1.3	1.5	1.8	1.9	2.2	2.8	3.3	3.8	4.7	5.2	6.0	6.4	7.2	7.6
rees	Branch Flow	2.0	2.6	3.3	4.4	5.2	6.6	7.5	9.4	12.0	15.0	18.0	24.0	30.0	34.0	37.0	43.0	47.0
Return	Regular 180 degree	0.9	1.2	1.6	2.1	2.4	3.1	3.6	4.4	5.9	7.3	8.9	12.0	14.0	17.0	18.0	21.0	23.0
Bends	Long radius 180 degree	1.1	1.3	1.6	2.0	2.3	2.7	2.9	3.4	4.2	5.0	5.7	7.0	8.0	9.0	9.4	10.0	11.0
	Globe	38.0	40.0	45.0	54.0	59.0	70.0	77.0	94.0	120.0	150.0	190.0.	260.0	310.0	390.0			
Values	Gate						2.6	2.7	2.8	2.9	3.1	3.2	3.2	3.2	3.2	3.2	3.2	3.2
Valves	Angle	15.0	15.0	17.0	18.0	18.0	21.0	22.0	285.0	38.0	50.0	63.0	90.0	120.0	140.0	160.0	190.0	210.0
	Swing Check	3.8	5.3	7.2	10.0	12.0	17.0	21.0	27.0	38.0	50.0	63.0	90.0	120.0	140.0			

# 20.0 555 Timer Design

$T = 0.693 (R_A + 2R_B)C$	(20.1)
$f = \frac{1}{T}$	(20.2)
$duty-cycle = \frac{(R_A + R_B)}{(R_A + 2R_B)} \cdot 100\%$	(20.3)
$T = period$ $f = frequency$ $R_A = resistance A$ $R_B = resistance B$ $C = capacitance$	

## 21.B Resistor Color Code



# 22.0 Speeds and Feeds

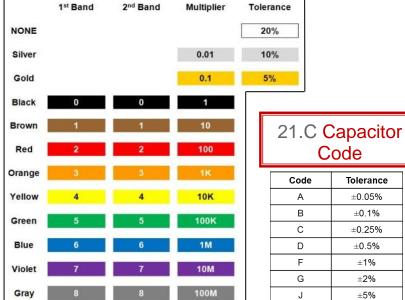
$N = \frac{CS(12\frac{in.}{ft})}{\pi d}$	(22.1)
$f_m = f_t \cdot n_t \cdot N$	(22.2)
Plunge Rate = $\frac{1}{2} \cdot f_r$ N = spindle speed CS = cutting speed d = diameter (in.) $f_m$ = feed rate (in./n $f_t$ = feed (in./tooth/r $h_t$ = number of teet	(rpm) d (ft/min) nin) rev)

# 21.A Boolean Algebra

Boolean Theorems						
X• 0 = 0	(21.1)					
X•1 = X	(21.2)					
X• X =X	(21.3)					
X • X̄=0	(21.4)					
X + 0 = X	(21.5)					
X + 1 = 1	(21.6)					
X + X = X	(21.7)					
$X + \overline{X} = 1$	(21.8)					
$\overline{\overline{X}} = X$	(21.9)					

Consensus T	heorems
$X + \overline{X}Y = X + Y$	(21.16)
$X + \overline{X}\overline{Y} = X + \overline{Y}$	(21.17)
$\overline{X} + XY = \overline{X} + Y$	(21.18)
$\overline{X} + X\overline{Y} = \overline{X} + \overline{Y}$	(21.19)
DeMorgan's Theorems	
DeMorgan's	Theorems
$\frac{\textbf{DeMorgan's}}{XY = X + Y}$	(21.20)
$\overline{XY} = \overline{X} + \overline{Y}$	(21.20) (21.21)
$\overline{XY} = \overline{X} + \overline{Y}$ $\overline{X+Y} = \overline{X} \cdot \overline{Y}$	(21.20) (21.21)

(21.12)



Code	Tolerance
А	±0.05%
В	±0.1%
С	±0.25%
D	±0.5%
F	±1%
G	±2%
J	±5%
K	±10%
M or NONE	±20%
N	±30%
Q	-10%, +30%
S	-20%, +50%
Т	-10%, +50%
Z	-20%, +80%

X + (Y + Z) = (X + Y) + Z	(21.13)
Distributive Law	
X(Y+Z) = XY + XZ	(21.14)
(X+Y)(W+Z) = XW+XZ+YW+YZ	(21.15)

## 23.0 G&M Codes

Associative Law

X(YZ) = (XY)Z

G00 = Rapid Traverse	(23.1)
G01 = Straight Line Interpolation	(23.2)
G02 = Circular Interpolation (clockwise)	(23.3)
G03 = Circular Interpolation (c-clockwise)	(23.4)
G04 = Dwell (wait)	(23.5)
G05 = Pause for user intervention	(23.6)
G20 = Inch programming units	(23.7)
G21 = Millimeter programming units	(23.8)
G80 = Canned cycle cancel	(23.9)
G81 = Drilling cycle	(23.10)
G82 = Drilling cycle with dwell	(23.11)
G90 = Absolute Coordinates	(23.12)
G91 = Relative Coordinates	(23.13)
M00 = Pause	(23.14)
M01 = Optional stop	(23.15)
M02 = End of program	(23.16)
M03 = Spindle on	(23.17)
M05 = Spindle off	(23.18)
M06 = Tool change	(23.19)
M08 = Accessory # 1 on	(23.20)
M09 = Accessory # 1 off	(23.21)
M10 = Accessory # 2 on	(23.22)
M11 = Accessory # 2 off	(23.23)
M30 = Program end and reset	(23.24)
M47 = Rewind	(23.25)

## 24.0 Aerospace

### Forces of Flight

$$C_D = \frac{2D}{A\rho v^2} \tag{24.1}$$

$$R_e = \frac{\rho vl}{\mu}$$
 (24.2)

$$C_{L} = \frac{2L}{A\rho v^2}$$
 (24.3)

$$M = Fd$$
 (24.4)

 $C_L$  = coefficient of lift

 $C_D$  = coefficient of drag

L = lift

D = drag

A = wing area

 $\rho$  = density

 $R_e$  = Reynolds number

v = velocity

I = length of fluid travel

 $\mu$  = fluid viscosity

F = force

m = mass

g = acceleration due to gravity

 $\dot{M} = moment$ 

#### **Propulsion**

$$F_N = W(v_j - v_o)$$
 (24.5)

$$I = F_{ave} \Delta t \tag{24.6}$$

$$F_{\text{net}} = F_{\text{avq}} - F_{\text{q}} \qquad (24.7)$$

$$a = \frac{v_f}{\Delta t}$$
 (24.8)

 $F_N$  = net thrust

W = air mass flow

v<sub>o</sub> = flight velocity

 $v_i$  = jet velocity

I = total impulse

F<sub>ave</sub> = average thrust force

 $\Delta t$  = change in time (thrust duration)

 $F_{net}$  = net force

 $F_{avg}$  = average force

 $F_a$  = force of gravity

v<sub>f</sub> = final velocity

a = acceleration

 $\Delta t$  = change in time (thrust duration)

NOTE:  $F_{ave}$  and  $F_{avg}$  are easily confused.

#### **Orbital Mechanics**

$$e = \sqrt{1 - \frac{b^2}{a^2}}$$
 (24.13)

$$T = 2\pi \frac{a^{\frac{3}{2}}}{\sqrt{\mu}} = 2\pi \frac{a^{\frac{3}{2}}}{\sqrt{GM}}$$
 (24.14)

$$F = \frac{GMm}{r^2}$$
 (24.15)

e = eccentricity

b = semi-minor axis

a =semi-major axis

T = orbital period

a = semi-major axis

 $\mu$  = gravitational parameter

F = force of gravity between two bodies

G = universal gravitation constant

M =mass of central body

m = mass of orbiting object

r = distance between center of two objects

#### Bernoulli's Law

$$\left(P_{S} + \frac{\rho v^{2}}{2}\right)_{1} = \left(P_{S} + \frac{\rho v^{2}}{2}\right)_{2}$$
 (23.16)

P<sub>S</sub> = static pressure

v = velocity

 $\rho$  = density

#### Atmosphere Parameters

T = 15.04 - 0.00649h

$$p = 101.29 \left[ \frac{(T + 273.1)}{288.08} \right]^{5.256}$$
 (24.18)

$$\rho = \frac{\rho}{0.2869(T + 273.1)} \tag{24.19}$$

T = temperature

h = height

p = pressure

 $\rho$  = density

## Energy

$$K = \frac{1}{2} mv^2$$
 (24.9)

$$U = \frac{-GMm}{R}$$
 (24.10)

$$E = U + K = -\frac{GMm}{2R}$$
 (24.11)

G = 
$$6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg} \times s^2}$$
 (24.12)

K = kinetic energy

m =mass

v = velocity

U = gravitational potential energy

G = universal gravitation constant

M =mass of central body

m = mass of orbiting object

R = Distance center main body to center of orbiting object

E = Total Energy of an orbit

(24.17)

### 25.0 USCS Soil Classification Chart

