

Activity 1.1.3 Gears Answer Key – VEX

Introduction

You do not have to look far to see gears. You might not think of an object such as a computer as having a lot of moving parts, but the CD tray on your computer is likely controlled by gears. A traditional watch is full of gears. The watch has one source of power or input that must move multiple hands continuously and at different speeds. Some watches also keep track of the day of the month. This may be low-tech by today’s standards, but imagine the challenge of choosing just the right gears to keep a watch synchronized. In a watch the gears are used to manipulate rotational speed. Gears are also used in many applications to control torque and rotational direction.

Equipment

* VEX POE kit gears and support pieces
* Calculator

Procedure

In this activity you will learn about gear ratios and how they affect speed and torque within asystem. You will also construct simple and compound gear systems.

Functions of Gears

* Gears change the speed of rotation.
* Gears change the direction of rotation.
* Gears change torque values.

Gear Ratios

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| --- | --- |
| By joining together two or more gears of different sizes, both the speed and the torque are changed from the input gear to the output gear. The larger gear within a system will always move slower and have more torque than the smaller gear. Gear Ratio (GR) is a comparison between the driver gear, also called the input (connected to the power source), and the gear being driven, or the output. Below are four ways to determine the gear ratio in figure 1. |  |

Method 1**:** The gear ratio can be determined by counting the number of teeth on each gear.The ratio is expressed by dividing the number of teeth on the output gear (nout)by the number of teeth on the input gear (nin).



Gear ratios are often expressed using a colon. In this example the ratiois 2:1 (pronounced two to one).The gear ratio of 2:1 indicates that the driver gear is half the size of the driven gear, and that the driver gear will make two revolutions for every one made by the driven gear.

Method 2: The gear ratio can be determined using the diameter of each gear.Assume that the diameter of gear A is 2.5 in. (din)**,** and the diameter of gear B is 5 in. (dout)**.**



Method 3: The gear ratio can be determined by recording and comparing the angular velocity or speed at which each gear is turning. The lower case Greek letter ωis used to represent angular velocity. A common way to measure angular velocity is using revolutions per minute (rpm)**.** Assume that the rpm of the input gear is 446 rpm and the rpm of the output gear is223 rpm.



Method 4: The gear ratio can be determined by recording the torque at each gear. Divide the torque at the output gear (τout) by the torque at the inputgear (τint). A common way to measure torque is to usefoot pounds(ft·lb). Assume that the torque force at the driver gear is 4 ft·lb and the force at the driven wheel is 8 ft·lb of torque.



The above equations all solve for the gear ratio of the driver gear to the driven gear.Based upon these formulas, the following is true.



Solving for Speed and Torque

In most applications you will know the speed and torque provided by your driver or input gear. You will mesh another gear to achieve a specific output speed or output torque to accomplish a task.Below are some examples that illustrate this.

Example 1:A motor is driving an axle with a 6 in. diameter drive gear. The speed of the motor is 20 rpm. A gear must be attached that increases the speed to 100 rpm. What size diameter should the attached gear be?





Example 2:A motor is driving an axle with a 30 teeth drive gear. You know that the maximum output torque of the motor is only 90 ft·lb. A gear must be attached that will increase the torque force to 300ft·lbin order to lift a heavy object. How many teeth should the attached gear have?





Gear Trains

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| --- | --- |
| A gear train consists of two or more gears assembled in order to transfer energy from one axis to others. |  |

Idler Gears

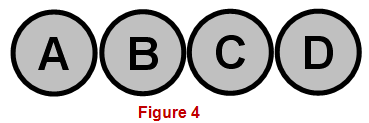
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| --- | --- |
| When two gears are meshed together, each will rotate in an opposite direction. If the desired rotation for two gears is the same, an idler gear is introduced. In Figure 3 the two outside gears will move at the same speed and direction and will have the same torque because of the idler gear between them. If they were attached without the idler gear, they would have matching speed and torque, yet would be rotating in opposite directions. |  |

Simple Gear Trains

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| --- | --- |
| A simple gear train connects two or more gears in a row, each gear having its own axle. |  |

Build a Simple Gear Train

In a group build a simple gear train that consists of four meshed gears each with its own axle. At least three gears should have different sizes. Once the gears are arranged, assume that the first gear, gear A, is the driver as seen in Figure 4. Attach a crank to gear A and compare the speeds of gears B, C, and D as you turn gear A.



Complete the following tables based upon the simple gear train that you created.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Number of Teeth Per Gear | | | | |
|  | A (nin) | B | C | D |
| n (teeth) | **10** | **20** | **30** | **20** |

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | B:A | C:B | D:C |  | |
| Gear Ratio (reduced) | 2:1 | 3:2 | 2:3 |
| Gear Ratios as Fractions |  |  |  | Product of Fractions | Final Gear Ratio |
|  | 2:1 |

By multiplying the gear ratios between each set, you discover the ratio between gears A and D.

Simple Gear Train Conclusion

1. How many times will gear A rotate compared to gear D? How does this compare to the gear ratio you just calculated in the table?

Gear A will rotate twice for every single rotation of gear D.

1. If 10 ft·lb of torque is applied at gear A, then what is the output at gear D?

|  |  |  |
| --- | --- | --- |
| Formula | Substitute / Solve | Final Answer |
|  |  |  |

1. How can you make gears A and D rotate in the same direction?

An idler gear placed anywhere between gears A and D would cause them to rotate in the same direction.

1. What will the gear ratio be if A is connected directly to D?

The gear ratio will be 2:1.

1. How does the ratio between A and D compare to the entire system?

The gear ratio between A and D is the same as the entire system.

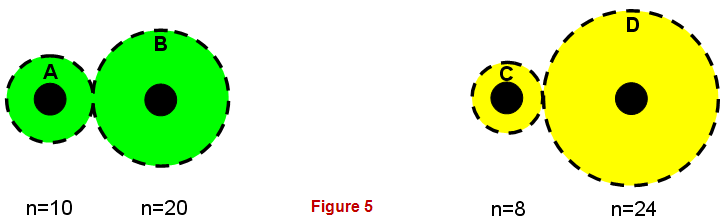
1. If gear D is the final output, or where the load is attached, then how did gears B and C impact the system?

Gears B and C do not change the gear ratio or rotation direction. They simply create space between gears A and D.

Compound Gear Trains

A compound gear train connects gears that may share axles or shafts. Two gears on the same shaft share the same torque and speed although they are different sizes. This allows more efficient manipulation of speed and torque throughout the system.

Figure 5 represents two simple gear trains and gear ratio for each set. The input for the first set is gear A. The input for the second set is gear C.





|  |  |
| --- | --- |
| Figure 6 represents the two simple gear trains above with gears B and C sharing the same shaft. Gear A is the driver. |  |

Solving For Compound Gear Trains

To solve for a compound gear train, determine the gear ratio of each simple gear train.Nextfind the product of all sets. We know from the previous example that the ratio between gears A and B is 1:2 and that the ratio between gears C and D is 1:3.

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| --- | --- |
|  | The gear ratio of 6:1 indicates that the driver gear A will make six revolutions for every one by the driven gear D, and that gear D will have 6 times more torque than gear A. |

Build a Compound Gear Train

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| In groups build a gear train that consists of four different-sized gears. The two gears in the middle must share the same shaft. Once the gears are arranged, assume that the driver is Gear A. Gear A is connected to gear B and will share the shaft with gear C, which is connected to gear D. Attach a crank to gear A and compare the speeds of gears B, C, and D as you turn A. |  |

Complete the following tables based upon the compound gear train that you created.

Student Answers will vary.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Number of Teeth Per Gear | | | | |
|  | A (nin) | B | C | D |
| n (teeth) | 10 | 30 | 20 | 40 |

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | B:A | D:C |  | |
| Gear Ratio (reduced) | 3:1 | 2:1 |
| Gear Ratios as Fractions |  |  | Product of Fractions | Final Gear Ratio |
|  | 6:1 |

Compound Gear Train Conclusion

1. How many times will gear A rotate compared to gear D?

Gear A will rotate 6 times for every 1 revolution of gear D.

1. If 7 ft·lb of torque is applied at gear A, then what is the output at gear D?

|  |  |  |
| --- | --- | --- |
| Formula | Substitute / Solve | Final Answer |
|  |  | 42.0ftlb |

1. Why might compound gear trains be better than two gears alone?

For larger gear ratios, one of the gears would have to be very large, whereas a compound gear train allows a larger gear ratio by stepping down ratios. Also, with a handful of gear sizes, different gear ratios can be attained by combining them as opposed to using specialized gears to attain a specific gear ratio.

1. Name and describe an application of a compound gear train.

Students should have a variety of answers.